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Use of a Self-Focusing Antenna for Low-Angle Tracking

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ABSTRACT

The response of a self-focusing antenna to two closely spaced point targets is investigated. The geometry simulated corresponds to the radar tracking of a low-flying target over a reflective surface. In one case the antenna consists of a vertical linear array of elements. When the conjugates of the incident signals are retransmitted at each element, after several iterations the antenna radiation pattern introduces significant discrimination against the weaker of the two unresolvable point targets. In the other case the same aperture is divided into two equal subapertures, and conjugate reflections are applied to the two subapertures rather than to each element. It is found that very nearly the same weak-target discrimination results. The implications of these results with regard to low-angle tracking are discussed.

AUTHORIZATION

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USE OF A SELF-FOCUSING ANTENNA FOR LOW-ANGLE TRACKING

INTRODUCTION

In the radar tracking of an object positioned over a reflective surface, a reflection from the surface may appear to the radar to be an image below the surface. (See Fig. 1, taken from Ref. 1.) If the energy from the image falls within the main lobe of the tracking radar, severe errors can result. There have been a number of attempts to reduce these errors (for some examples see Ref. 2), but the problem is still an open one. This report discusses the feasibility of using an adaptive or self-focusing antenna for low-angle tracking.

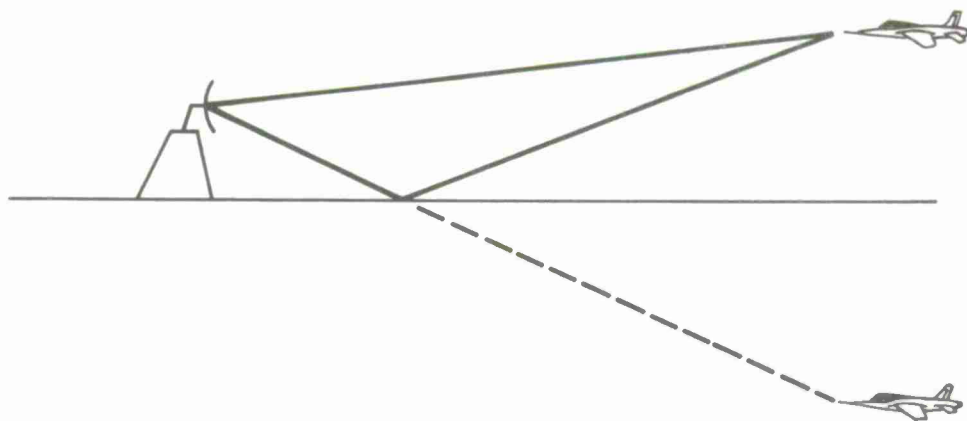


Fig. 1 — Reflection from the surface appears as a target image

A self-focusing antenna uses the unique properties of conjugate reflections to return, as a coherent wavefront, an incident wavefront in the direction from whence it came. If the incident waveform is backscatter from two point targets, the retransmitted wave is directed toward the stronger target, thus discriminating against the weaker target (3-5). It is this discrimination against a weaker target which could render this technique useful for low-angle tracking.

At the time this investigation was begun, it was well known (5) that discrimination against a weaker target would occur if sufficient aperture were available to resolve the targets. However, if self-focusing is to be useful for low-angle tracking, discrimination against a weaker target, i.e., the image, must occur when the target and image lie within the main-lobe beamwidth. This is the main question to which the investigation reported on here was addressed.

MATHEMATICAL DEVELOPMENT

General Case

A computer simulation program, provided as an appendix, was developed to calculate and plot the radiation intensity at points in the target/image plane. Plotting the radiation pattern proved to be a convenient way to analyze the behavior of the self-focusing antenna for closely spaced targets. The geometry used in the simulation program is shown in Fig. 2. The self-focusing antenna consists of a linear aperture D sampled at every half wavelength. The sample points x_i are a measure of distance above the reference plane (ocean surface). The number of aperture samples actually used in the program was 51. The distance from the antenna to the target axis is R , and the target height is h_t . The radiation intensity is calculated at discrete points u_j along the target/image axis. The distance d_{ij} from a sample point x_i along the aperture to a sample point u_j on the target/image axis is

$$d_{ij} = \sqrt{R^2 + (x_i - u_j)^2}, \quad (1)$$

and the corresponding electrical length of that path is

$$\phi_{ij} = \frac{2\pi}{\lambda} d_{ij}, \quad (2)$$

where λ is the wavelength. Neglecting all attenuation losses, a complex transmission coefficient Γ_{ij} for the ij th path can be defined as the complex exponent ϕ_{ij} , i.e.,

$$\Gamma_{ij} = e^{j\phi_{ij}}, \quad j > \frac{N}{2}, \quad (3a)$$

where N is the total number of sample points along the target/image axis. For paths which include a surface reflection, an additional 180° phase shift is included, i.e.,

$$\Gamma_{ij} = e^{j(\phi_{ij} + \pi)}, \quad j = 1, 2, \dots, \frac{N}{2}. \quad (3b)$$

The attenuation of the surface reflection could be accounted for in the coefficient Γ_{ij} ; however, in the present program this attenuation is accounted for by reducing the cross section of the image. There is a radar cross section $\rho(u_j)$ (a complex number) associated with each sample point along the target/image axis, but only the nonzero points correspond to the target and its image.

The process is begun by illuminating each point along the target axis with some initial function $B_0(u_j)$ which was taken to be uniform, i.e., unity for all j . On the first iteration, the wave back at the i th sample point in the aperture is given by

$$A_I(x_i) = \sum_j B_0(u_j) \rho(u_j) \Gamma_{ij}. \quad (4)$$

The paths are assumed to be reciprocal, that is $\Gamma_{ji} = \Gamma_{ij}$. At each point x_i in the aperture, the complex conjugate $A_I^*(x_i)$ is generated and transmitted. This is the essential operation constituting self-focusing. In practical terms, at each sample point in the aperture, the phase of the received signal is reversed and then retransmitted. Back at the target/image axis, the wave at each point is

$$B_1(u_j) = \sum_i A_1^*(x_i) \Gamma_{ij}, \quad (5)$$

or substituting Eq. (4) into Eq. (5),

$$B_1(u_j) = \sum_i \left[\sum_k B_0^*(u_k) \rho^*(u_k) \Gamma_{ik}^* \right] \Gamma_{ij}. \quad (6)$$

The subscript one on $B_1(u_j)$ indicates the first iteration. After iterating this process a number of times, results converge to form the adapted or focused pattern.

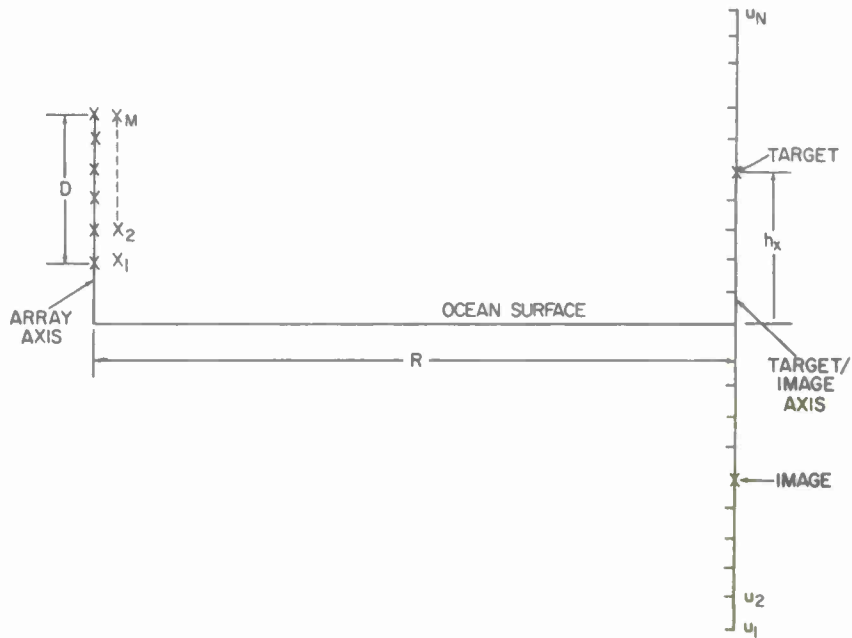


Fig. 2 — Geometry used in simulation program

Case of Two Subapertures

A variation on the previous approach, which can lend considerable practicability to the concept of self-focusing, involves the phasing of two subapertures rather than the phasing of each element of an array. Two subapertures are formed by dividing the aperture D in Fig. 2 into halves. Now instead of retransmitting the conjugate of the signals received at each sample point in the aperture, the average phase across the aperture is computed, conjugated, and retransmitted. On retransmission the phase across the subaperture is constant. In effect then, the phase distribution across the entire aperture is replaced by a two-step approximation. The average signal for the first subaperture is

$$E_k = \frac{2}{M} \sum_{i=1}^{M/2} A_k(x_i), \quad (7)$$

where M is the total number of sample points in the aperture D and k is the iteration number. For the second subaperture,

$$F_k = \frac{2}{M} \sum_{i=\frac{M}{2}+1}^M A_k(x_i). \quad (8)$$

Then the wave at a point on the target/image axis is (k th iteration)

$$\begin{aligned} B_k(u_j) &= \sum_{i=1}^{M/2} E_k^* \Gamma_{ij} + \sum_{i=\frac{M}{2}+1}^M F_k^* \Gamma_{ij} \\ &= E_k^* \sum_{i=1}^{M/2} \Gamma_{ij} + F_k^* \sum_{i=\frac{M}{2}+1}^M \Gamma_{ij}. \end{aligned} \quad (9)$$

Some performance degradation is expected to result from this approach, but if the phase distribution across the entire aperture is benign enough, very little degradation will occur. This is the second major question to which this brief study was directed.

RESULTS

The magnitude $|B_k(u_j)|$ of the wave is computed and plotted at 51 points along the target/image axis. (The plot routine interpolates linearly between computed points.) In Fig. 3 the distance between the target and its image corresponds approximately to the 3-dB beamwidth of the antenna. The arrows at 1000 m and -1000 m locate the target* and image respectively and also indicate their relative strengths. A distinct increase in image discrimination can be seen for the second iteration (Fig. 3b), and for the fifth iteration (Fig. 3c) the image is completely nulled out. Positioning of a null exactly on the image is not possible in general, but it occurs here because the separation between the target and image corresponds to the distance between the peak of the antenna lobe and the first null. The pattern has converged to its final value by the tenth iteration.

Figure 4 corresponds to a half-beamwidth separation between the target and image. An improvement in image discrimination can be seen on each iteration until the final value is reached. A close examination of the plots reveals that little main-lobe distortion occurs; however, the primary effect is a shifting of the main-lobe axis. The final alignment of the radiation pattern is such that the target is strongly favored while at the same time the image is illuminated minimally.

For the low-angle-tracking problem, a more realistic ratio of target strength to image strength is 1 to 0.9. This case is plotted in Fig. 5 for a half-beamwidth separation between target and image. Convergence of the pattern is considerably slower than in Figs. 3 and 4 where the relative strengths are 1 to 0.5. By iteration 30 the discrimination against the

*For an S-band ($\lambda = 0.33$ ft) radar and a 6.6 ft aperture, this corresponds to a range of 22 naut. mi.

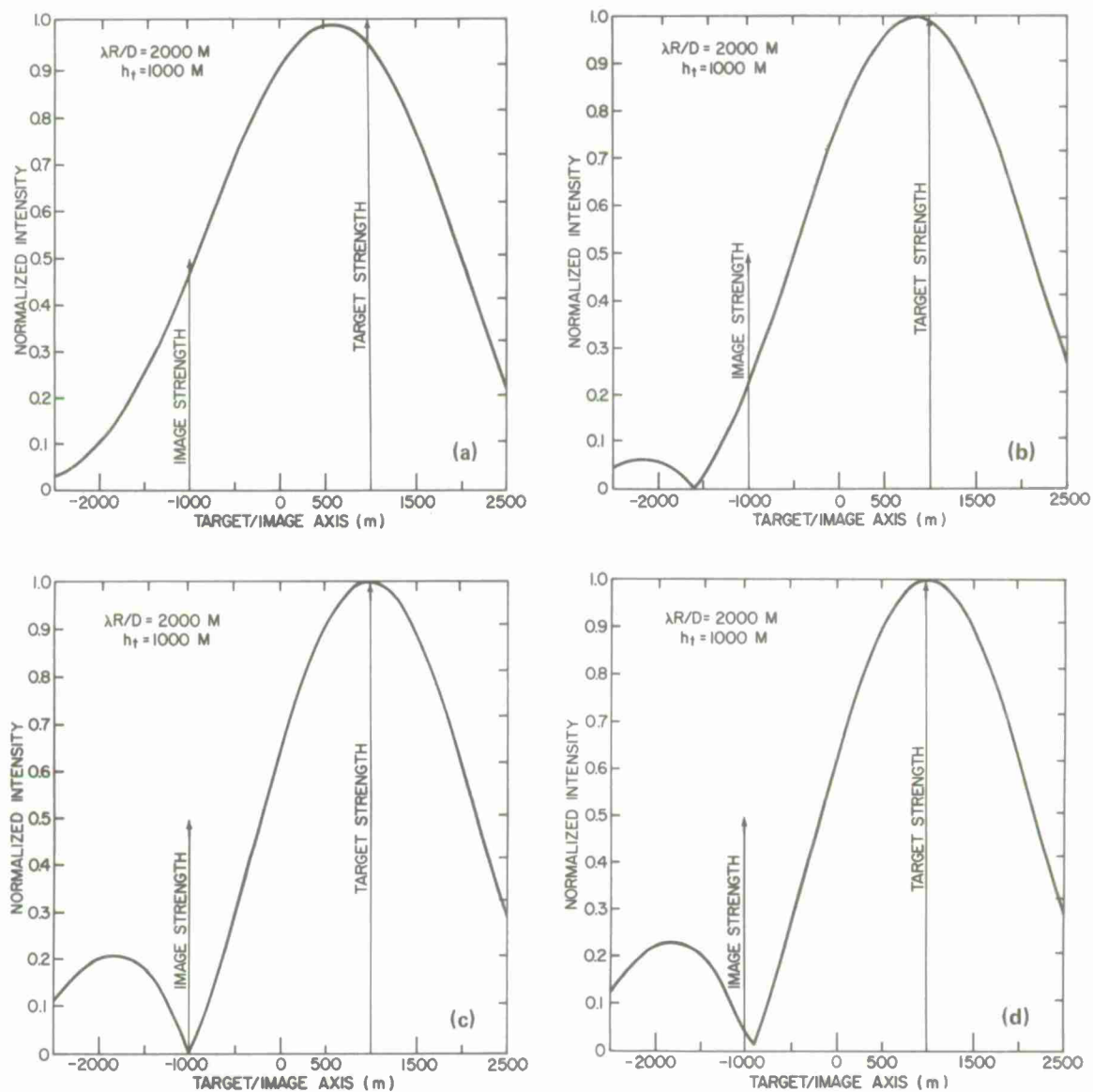


Fig. 3 — Pattern of a self-focusing antenna when the target/image spacing is one beam-width. (a) One iteration, (b) Two iterations, (c) Five iterations, (d) Ten iterations.

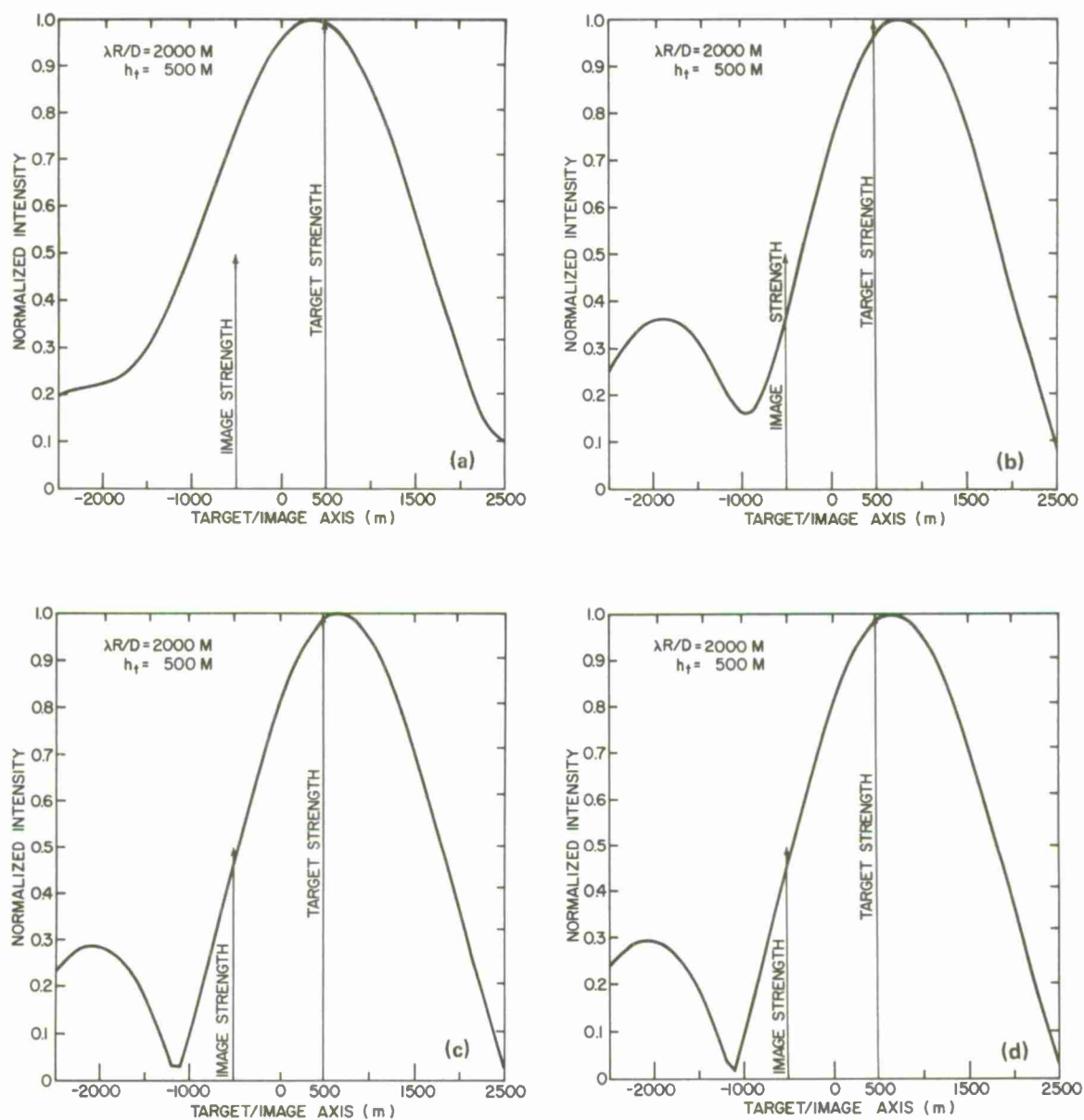


Fig. 4 — Pattern of a self-focusing antenna when the target/image spacing is half beam-width. (a) One iteration, (b) Two iterations, (c) Five iterations, (d) Ten iterations.

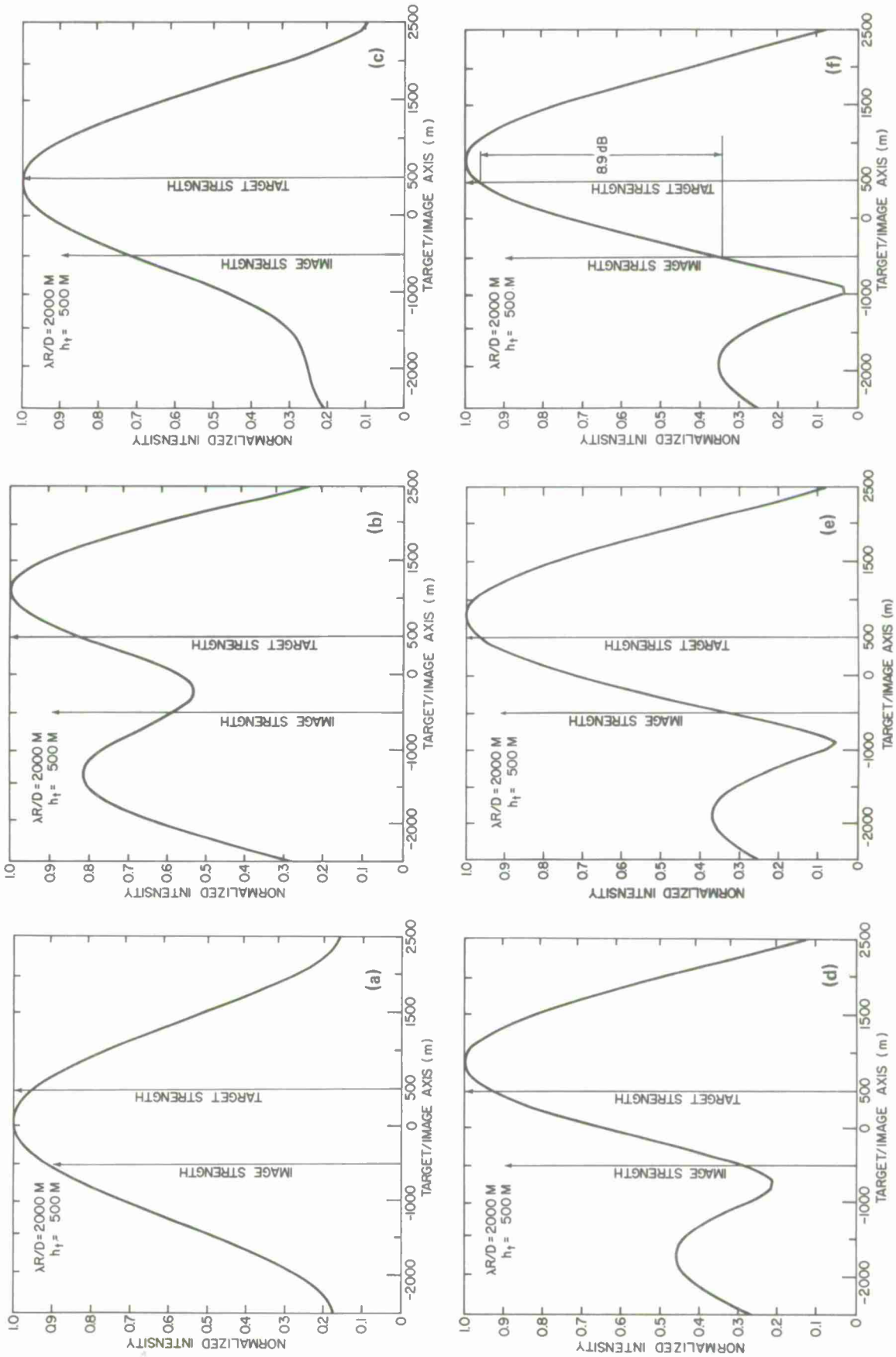


Fig. 5 — Pattern of a self-focusing antenna when the target/image spacing is half beamwidth and the relative image strength is 0.9. (a) One iteration, (b) Two iterations, (c) Five iterations, (d) Ten iterations, (e) Twenty iterations, (f) Thirty iterations.

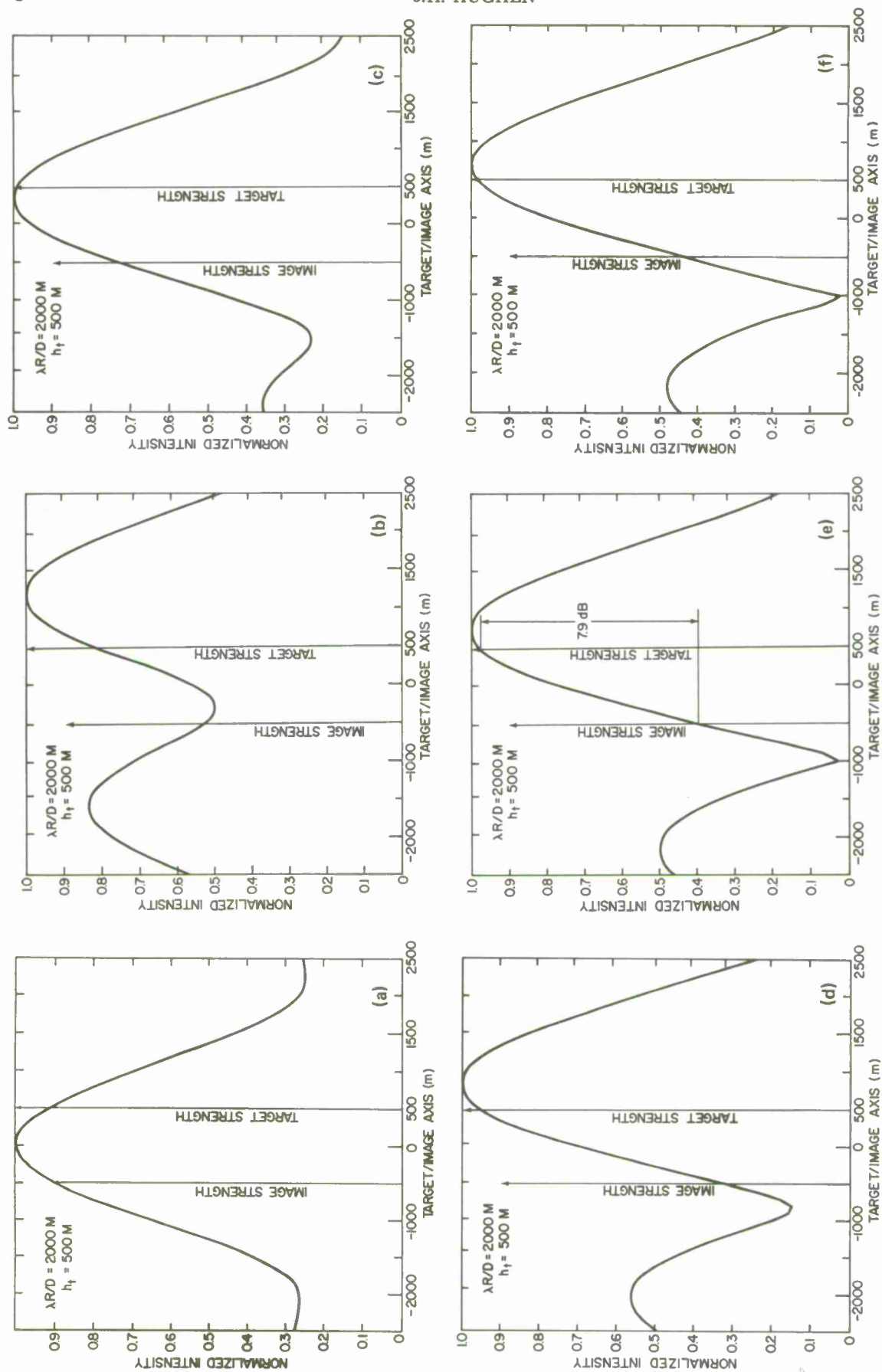


Fig. 6 — Pattern for self-focusing applied to two subapertures. The target/image spacing is half-beamwidth and the relative image strength is 0.9. (a) One iteration, (b) Two iterations, (c) Five iterations, (d) Ten iterations, (e) Twenty iterations, (f) Twenty-nine iterations.

image is 8.9 dB. Although not shown in the figure, after iteration 29 the discrimination was 8.4 dB, and the effect is somewhat oscillatory. The final value would be about 8.7 dB. It is interesting that this is somewhat better than the final value in Fig. 4d, which was 6.75 dB.

Finally, in Fig. 6 the results obtained for the two subapertures are shown. The results in Fig. 6 are extremely encouraging in that the final value of discrimination is about 7.5 dB or only about 1.25 dB worse than the results for the full-aperture case of Fig. 5. Convergence is slow in Fig. 6, but it does not appear to be any slower than in Fig. 5. There is some cause for concern in Figs. 5 and 6 in that a high side lobe appears below the image in both cases. The effect of this side lobe is to increase the sea-clutter level. It is possible that this clutter may correspond to a range cell outside the cell of interest, in which case the effect may be negligible. On the other hand, the effect of the clutter on the focused pattern itself is unknown.

CONCLUSIONS

It has been demonstrated that a self-focusing antenna can discriminate against the weaker of two targets even when the target spacing is such that both targets are well within the beamwidth of the antenna. Furthermore, the results obtained indicate that it may be possible to achieve good image discrimination in low-angle tracking using two subapertures rather than phasing the individual elements of an array.

The results of this brief study are not sufficient to conclude that a self-focusing antenna would be useful for low-angle tracking. This writer feels that two additional questions must be considered before even the most tentative conclusion can be drawn. First, the effect of target motion needs to be considered. This can be investigated by a rather straightforward modification to the existing computer program.

The more critical question regards the actual tracking error. To investigate this question, a suitable tracking algorithm must be developed and analyzed. At this point it is not perfectly clear how to use the self-focusing technique most effectively. However, an approach which appears promising is to use self-focusing in conjunction with monopulse: the target would be illuminated by the self-focusing antenna, and tracking could be accomplished by a separate monopulse system operating in a receive-only mode.

ACKNOWLEDGMENT

This study owes its existence to Dr. M. I. Skolnik. The idea of using self-focusing for low-angle tracking is his, and I am grateful for having had the opportunity to work on it.

My deepest appreciation goes to Dr. W. M. Waters. During the brief period of this study, I spent several hours in discussion with him. His explanations and interest were indispensable. It was in fact his computer program which I used with minor modifications, and the mathematical development presented here is from his work, Ref. 5.

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Appendix

COMPUTER SIMULATION PROGRAM FOR THE SELF-FOCUSING PROBLEM

```

PROGRAM C
COMPLEX      CI(60),CA(60),A(60),AO,GAMMA,DUM,Z(60,60),FAC(5,5)
1,AUX(60,60),RHO(60),BUM
DIMENSION X(60),U(60),COSPHI(60,60),SINPHI(60,60),ANORM(60),
1AMAG(60),NPLOT(20),PLTARRAY(254)
CALL PLOTS(PLTARRAY,254,1)
READ 2,XMIN,XMAX,DELX
2 FORMAT(6F10.2)
READ 2,UMIN,UMAX,DELU
READ 3,R,NMAX,WLAM
3 FORMAT(F10.2,I5,F10.2)
READ 4,ICASE,NP,(NPLOT(I),I=1,NP)
4 FORMAT(10(I5))

      ICASE=CAWE NO.,NP=NO. OF PLOTS,NPLOT=ITERATON FOR PLOTS,NMAX=NO OF IT.

PI=3.14159265
AO=(1.,0.)
GAMMA=(1.,0.)

      COMPUTE X-ARRAY

PRINT 5,XMIN,XMAX,DELX
5 FORMAT(1H1,15X,*XMIN=*,F10.2,15X,*XMAX=*,F10.2,15X,*DELX=*,F10.2)
PRINT 6,UMIN,UMAX,DELU
6 FORMAT(/15X,*UMIN=*,F10.2,15X,*UMAX=*,F10.2,15X,*DELU=*,F10.2)
XL0D=WLAM/(XMAX-XMIN)
ELANG=UMAX/R
XLUM=XL0D*R
PRINT 7,R,NMAX,WLAM
7 FORMAT(/15X,*RANGE=*,F10.2,*METERS      NMAX=*,I3,5X,*LAMBDA=*,
1F6.2,*CM*)
PRINT 8,XL0D,ELANG,XLUM
8 FORMAT(/10X,*L0D=*,E10.3,5X,*EL ANGLE=*,E10.3,5X,*LR/D=*,E10.3)
I=1
X(I)=XMIN
10 I=I+1
X(I)=X(I-1)+DELX
IF(X(I)-XMAX)10,11,11
11 IMAX=I

      COMPUTE U-ARRAY$JMAX

NTARG=0
J=1
U(J)=UMIN
RHO(J)=(0.,0.)
12 J=J+1
U(J)=U(J-1)+DELU
IF(U(J).EQ.-500.)14,153
153 IF(U(J).EQ.500.)15,60
15 RHO(J)=(1.,0.)
JTARG=J
GO TO 16
14 RHO(J)=(.9,0.)
JIMAG=J
16 NTARG=NTARG+1
GO TO 17
60 RHO(J)=(0.,0.)

```

```

17 IF (U(J)-UMAX)12,18,18
18 JMAX=J

```

COMPUTE SIN&COS OF PHI

```

JHALF=JMAX/2
DO 19 I=1,IMAX
DO 19 J=1,JMAX
PHI=PI*2./WLAM*SQRT(R**2+(X(1)-U(J))**2)
IF (J.LT.JHALF)PHI=PHI+PI
COSPHI(1,J)=COS(PHI)
19 SINPHI(I,J)=SIN(PHI)

```

COMPUTE COM P ES VALUES OF GAMMA

```

DO 20 I=1,IMAX
DO 20 J=1,JMAX
DUM=CMPLX(COSPHI(1,J),SINPHI(1,J))
20 Z(1,J)=GAMMA*DUM

```

CLEAR AN(U) ARRAY ONCE ONLY FOR ALL ITERATIONS

```

DO 21 J=1,JMAX
21 A(J)=(0.,0.)

```

CLEAR IN(U) ARRAY (TARGET REFLECTION) AND RECEPTION ARRAYS FOR EACH ITERATION

```

DO 22 J=1,JMAX
22 CI(J)=(0.,0.)
DO 23 I=1,IMAX
23 CA(I)=(0.,0.)

```

COMPUTE FIRST ITERATION OF AN(U),IN(U)\$AN(X)

```

IHALF=IMAX/2
N=1
DO 24 J=1,JMAX
24 CI(J)=RHO(J)*AO
DO 25 I=1,IMAX
DO 25 J=1,JMAX
25 CA(I)=CA(I)+CI(J)*Z(I,J)
EQ 1 IN WATERS'12
BUM=(0.,0.)
DUM=(0.,0.)
DO 128 I=1,IHALF
128 DUM=DUM+CA(I)
ME=IHALF+1
DO 129 I=ME,IMAX
129 BUM=BUM+CA(I)
BUM=CONJG(BUM)/(IMAX-IHALF)
DUM=CONJG(DUM)/IHALF
DO 130 I=1,IHALF
130 CA(I)=DUM
DO 131 I=ME,IMAX
131 CA(I)=BUM
DO 26 J=1,JMAX
DO 26 I=1,IMAX
26 A(J)=A(J)+CA(I)*Z(I,J)

```

GO TO 32

CLEAR IN(U)\$AN(X) ARRAYS \$ ITERATE

```

37 DO 27 J=1,JMAX
27 CI(J)=(0.,0.)
DO 28 I=1,IMAX
28 CA(I)=(0.,0.)
DO 29 J=1,JMAX
29 CI(J)=RHO(J)*A(J)
DO 30 I=1,IMAX
DO 30 J=1,JMAX
30 CA(I)=CA(I)+CI(J)*Z(I,J)
BUM=(0.,0.)
DUM=(0.,0.)
DO 138 I=1,IHALF
138 DUM=DUM+CA(I)
DO 139 I=ME,IMAX
139 BUM=BUM+CA(I)
DUM=CONJG(DUM)/IHALF
BUM=CONJG(BUM)/(IMAX-IHALF)
DO 140 I=1,IHALF
140 CA(I)=DUM
DO 141 I=ME,IMAX
141 CA(I)=BUM
DO 40 J=1,JMAX
40 A(J)=(0.,0.)
DO 31 J=1,JMAX
DO 31 I=1,IMAX
31 A(J)=A(J)+CA(I)*Z(I,J)
32 PRINT 1003,ICASE,NTARG,N
1003 FORMAT(14X,*ADAPTIVE ARRAY PHASING PROBLEM*,//,17X,*CASE*,I2,2X,I3
1,*POINT TARGETS*,//20X,*ITERATION NUMBER*,I3,//13X,*U(J)*,17X,
2*NORMALIZED AN(U)*,//)
AMAX=0.
DO 33 J=1,JMAX
AMAG(J)=CABS(A(J))
33 AMAX=MAX1F(AMAG(J),AMAX)

NORMALIZE AN(U) $ PRINT OUT U $ AN(U)

DO 34 J=1,JMAX
ANORM(J)=AMAG(J)/AMAX
34 CONTINUE
DISCRM=20.*ALOG10(ANORM(JTARG)/ANORM(JIMAG))
PRINT 1005,DISCRM
1004 FORMAT(11X,F8.2,10X,E20.8)
1005 FORMAT(5X,*IMAGE DISCRIMINATION*,F6.2,*DB*)
DO 50 I=1,NP
IF(N.EQ.NPLOT(I))51,50
51 CALL GRAPHPLT(ANORM,PLTARRAY,JMAX)
50 CONTINUE
IF(N=NMIX)35,36,36
35 N=N+1
GO TO 37
36 CONTINUE
CALL STOPPLOT
END

```



```
SUBROUTINE GRAPHPLT(ANORM,PLTARRAY,JMAX)
DIMENSION ANORM(1),PLTARRAY(254)
X=0.
Y=0.
IP=-3
CALL PLOT(X,Y,IP)
IP=2
DO 100 I=1,10
X=X+1.
CALL PLOT(X,Y,IP)
Y=.1
CALL PLOT(X,Y,IP)
Y=0.
CALL PLOT(X,Y,IP)
100 CONTINUE
IP=3
X=0.
Y=0.
CALL PLOT(X,Y,IP)
DO 200 I=1,10
IP=2
Y=Y+1.
CALL PLOT(X,Y,IP)
X=.1
CALL PLOT(X,Y,IP)
X=0.
CALL PLOT(X,Y,IP)
200 CONTINUE
CALL PLOT(4.,0.,3)
CALL PLOT(4.,9.,2)
CALL PLOT(4.,0.,2)
CALL PLOT(6.,0.,3)
CALL PLOT(6.,10.,2)
CALL PLOT(6.,0.,2)
X=0.
IP=3
Y=0.
CALL PLOT(X,Y,IP)
DO 300 J=1,JMAX
IP=2
X=.2*(J-1)
Y=10.*ANORM(J)
CALL PLOT(X,Y,IP)
300 CONTINUE
CALL PLOTS(0,0)
CALL PLOTS(0,0)
RETURN
END
```

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		ROLE	WT	ROLE	WT	ROLE	WT
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